# ECLIPSING BINARY STARS IN THE LARGE AND SMALL MAGELLANIC CLOUDS FROM THE MACHO PROJECT: THE SAMPLE

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### ABSTRACT

We present a new sample of 4634 eclipsing binary stars in the Large Magellanic Cloud (LMC), expanding on a previous sample of 611 objects and a new sample of 1509 eclipsing binary stars in the Small Magellanic Cloud (SMC), that were identified in the light-curve database of the MACHO project. We perform a cross-correlation with the OGLE-II LMC sample, finding 1236 matches. A cross correlation with the OGLE-II SMC sample finds 698 matches. We then compare the LMC subsamples corresponding to the center and periphery of the LMC and find only minor differences between the two populations. These samples are sufficiently large and complete that statistical studies of the binary star populations are possible.

Key words: binaries: eclipsing — Magellanic Clouds — surveys

Online material: machine-readable tables, tar file

# 1. INTRODUCTION

Eclipsing binary stars (EBs) are important for astrophysical research in many ways. They can be used to obtain accurate estimates of star masses and radii (Andersen 1991 and references therein). Precise determination of stellar parameters can, in turn, be used to put theories of stellar structure and evolution to a stringent test by comparing measured parameters with theoretical predictions (Lastennet & Valls-Gabaud 2002; Lastennet et al. 2003 and references therein).

EBs may also be used for distance determination, and this use goes back several decades; its history is reviewed by Kruszewski & Semeniuk (1999). Since Stebbins (1911) used an estimate of the parallax to  $\beta$  Aurigae to infer the surface brightness of both its components, it has been known that a good photometric light curve plus a double-line spectroscopic orbit allows a simple geometric relationship between the surface brightnesses of the stars and the distance to the EB; Stebbins (1911), however, had no way at the time to make the reverse "surface brightness to distance" inference, and his paper does not mention this possibility. After Stebbins (1911), other early papers (Gaposchkin 1933, 1938, 1940; Woolley 1934; Pilowski 1936; Kopal 1939) used parallaxes obtained independently to estimate surface brightnesses, but, as remarked by Kruszewski & Semeniuk (1999), these pioneers surely knew of the potential of this technique to estimate distances. Modern analyses of EBs have usually focused on this technique (e.g., Andersen 1991). The method affords high precision due to its purely geometric nature and has been applied by a number of authors to determine the distance to the Large Magellanic Cloud (LMC) using HV 2274 (Udalski et al. 1998a; Guinan et al. 1998; Nelson et al. 2000; Groenewegen & Salaris 2001), HV 982 (Fitzpatrick et al. 2002), EROS 1044 (Ribas et al. 2002), and HV 5936 (Fitzpatrick et al. 2003); an attempt to use EBs to determine the distance to M31 is currently underway (Ribas et al. 2003), and the DIRECT project is attempting to measure the distance to M31 and M33 via EBs and Cepheids (Kaluzny et al. 1998; Bonanos et al. 2003; Bonanos 2005). Other recent examples include Michalska & Pigulski (2005), who present a sample of detached binaries in the LMC for distance determination, and Ribas et al. (2005), who present the first determination of the distance and properties of an EB in M31; North (2006) presents a sample of EBs with total eclipses in the LMC suitable for spectroscopic studies. In general, it is important that distances be determined using a large sample of EBs to minimize the impact of systematic errors. A recent collection of references on extragalactic binaries can be found in Ribas & Gimenez (2004).

Large-scale surveys to detect gravitational microlensing events have identified and collected light curves for large numbers of variable stars in the bulge of the Milky Way and in the Magellanic Clouds. Eclipsing binary stars comprise a significant fraction of these collections. The MACHO collaboration<sup>1</sup> has presented a

<sup>&</sup>lt;sup>1</sup> See http://www.macho.mcmaster.ca.

sample of 611 EBs in the LMC with preliminary analyses of their orbits (Alcock et al. 1997a). A catalog of 3031 EBs in the LMC found in the MACHO database has been just published by Derekas et al. (2007); this catalog was compiled by analyzing a list of 6835 stars classified as possible EBs in the MACHO database; a cross-correlation between these 6835 stars and our sample finds just 1987 matches; thus, at least about 2700 EBs in our catalog are new identifications. The 6835 classified as possible EBs were found in regions of parameter space such as color, magnitude, and period, where one does not expect to find pulsating variables, and therefore the detected variability of these stars was tentatively ascribed to eclipses. Regions where pulsating variables could exist were not considered while making this preliminary classification, and EBs were therefore not included in the list. In our search we did not rely primarily on cuts in parameter space, and we did not exclude a priori regions of this space where pulsating variables are present; therefore, we were able to classify many EBs in these regions that were not included in the preliminary classification. The OGLE collaboration<sup>2</sup> has introduced a sample of 2580 EBs in the LMC (Wyrzykowski et al. 2003) and 1351 EBs in the Small Magellanic Cloud (SMC; Wyrzykowski et al. 2004). Both samples were selected from their catalog of variable stars in the Magellanic Clouds (Żebruń et al. 2001) compiled from observations taken during the second part of the project (OGLE-II: Udalski et al. 1997) and reduced via difference image analysis (DIA; Żebruń et al. 2001). An earlier sample of 79 EBs in the bar of the LMC was presented by the EROS collaboration<sup>3</sup> (Grison et al. 1995). Other large variable-star data sets are being produced by surveys not specifically designed to detect gravitational microlensing, such as the All Sky Automated Survey (ASAS; Pojmański 1997).<sup>4</sup>

The availability of large samples of EBs (and the even larger ones that can be found by future surveys such as Pan-STARRS<sup>5</sup> and LSST<sup>6</sup>) can have an important impact on stellar astrophysics. This impact can arise in two qualitatively different approaches. First, a large catalog allows the discerning researcher to select carefully a few EBs for detailed follow-up study; the distance estimation described above is an example of this. Second, statistical analyses of an entire population become possible when a large collection is assembled; such analyses of EBs have not previously been possible. To fulfill this promise there are challenges to overcome, including finding EBs in large data sets and automating their analysis. With regard to the first task, the discovery problem is complicated by the fact that EBs do not have clear relationships between their parameters (period, luminosity, and color), as do the major classes of pulsating variables. This makes it difficult to find them via simple and well-understood cuts in parameter space. The first step toward automated discovery is thus to have a large sample of data on which to experiment with search techniques. This nontrivial exercise in mining large data sets can be useful for future surveys that are not necessarily aimed at binary star research.

An example is given by Wyrzykowski et al. (2003, 2004), who employ an artificial neural network to identify EBs in the OGLE-II LMC and SMC samples, but more needs to be done. With regard to the *analysis* of EBs, the traditional approach has been to carefully analyze individual systems with the help of dedicated computer codes such as the Wilson-Devinney code (WD; Wilson & Devinney 1971; Wilson 1979). This becomes impracticable when many thousands of stars are involved and an automated approach is required. The light curves in a previous sample of 1459 EBs in the SMC found by OGLE-II (Udalski et al. 1998b) were systematically solved by Wyithe & Wilson (2001, 2002) using an automated version of the WD code; the ASAS collaboration has developed an automated classification algorithm for variable stars based on Fourier decomposition (Pojmański 2002); Devor (2005) found and analyzed 10,000 bulge EBs from OGLE-II using DEBiL,<sup>7</sup> an EB analysis code that allows automated solutions of large EB data sets and works best for detached EBs; a genetic algorithm—based approach to finding good initial parameters for WD is described in Metcalfe (1999).

This paper is the first of a series of papers aimed at describing the EB samples in the MACHO database and is organized as follows: § 2 introduces the LMC and SMC samples; § 3 describes the color-magnitude diagram (CMD) and the color-period diagram, pointing out significant features in them; § 4 compares the LMC and SMC samples; § 5 describes the results of the cross-correlation with the OGLE LMC and SMC samples; and § 6 reports where and in what form the data presented in the paper can be accessed online.

## 2. THE SAMPLES

### 2.1. The MACHO Project

The MACHO project was an astronomical survey whose primary aim was to detect gravitational microlensing events of background sources by compact objects in the halo of the Milky Way. The gravitational background sources were located in the LMC, the SMC, and the bulge of the Milky Way; more details on the detection of microlensing events can be found in Alcock et al. (2000a and references therein). Observations were carried out from 1992 July to 1999 December with the dedicated 1.27 m telescope of Mount Stromlo, Australia, using a  $2 \times 2$  mosaic of  $2048 \times$ 2048 CCD in two bandpasses simultaneously. These are called MACHO "blue," hereafter indicated by  $V_{\text{MACHO}}$ , with a bandpass of ~440-590 nm; and MACHO "red," hereafter indicated by  $R_{\text{MACHO}}$ , with a bandpass of ~590–780 nm. These widths are between the half-response points as estimated from Figure 1 of Alcock et al. (1999). The bandpasses and the transformations to standard Johnson V and Cousins R bands are described in detail in Alcock et al. (1999); see in particular their Figure 1 for the instrumental throughput of the two MACHO bands. Each MACHO object is identified by its field number (1-82 for the LMC, 201-213 for the SMC), its tile number (which can overlap more than one field), and its sequence number in the tile. These form the socalled MACHO Field. Tile. Sequence (FTS), which is used in this paper to label EBs. Note that, since some overlap exists between fields, one star may have two or more FTS identifiers.

### 2.2. The Large Magellanic Cloud Sample

The LMC sample we present comprises 4634 EBs selected by a variety of methods which we describe in this section; the sample includes the 611 EBs described in Alcock et al. (1997a). The LMC magnitudes quoted in this paper have been obtained by using the following transformation:

$$V = V_{\text{MACHO}} + 24.22 \text{ mag} - 0.18(V_{\text{MACHO}} - R_{\text{MACHO}}),$$
  

$$R = R_{\text{MACHO}} + 23.98 \text{ mag} + 0.18(V_{\text{MACHO}} - R_{\text{MACHO}}).$$
 (1)

From now on we use V, R, and V - R to refer to standard magnitudes obtained from  $V_{\text{MACHO}}$  and  $R_{\text{MACHO}}$  via equation (1)

<sup>&</sup>lt;sup>2</sup> See http://sirius.astrouw.edu.pl/~ogle/.

See http://eros.in2p3.fr.

See http://www.astrouw.edu.pl/~gp/asas/asas.html.

 <sup>&</sup>lt;sup>5</sup> See http://pan-starrs.ifa.hawaii.edu/public/.
 <sup>6</sup> See http://www.lsst.org/lsst\_home.shtml.

<sup>&</sup>lt;sup>7</sup> See http://www.cfa.harvard.edu/~jdevor/DEBiL.html.

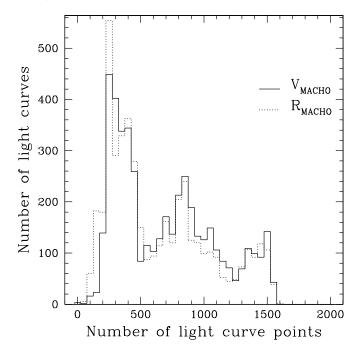


Fig. 1.—Histograms of the number of light-curve points for both bands for the LMC sample. The first peak corresponds to objects in the LMC periphery, which was observed less often than the center, and the other two peaks to the regions in and near the central bar.

for the LMC and equation (2) for the SMC, with *no correction for reddening*; we also use  $V_{\text{MACHO}}$  and  $R_{\text{MACHO}}$  to indicate instrumental magnitudes. The observations number in the several hundreds in both bandpasses for most light curves; Figure 1 shows histograms of the number of light-curve points of the EBs in both bands; the  $V_{\text{MACHO}}$  band has on average more observations than the  $R_{\text{MACHO}}$  band because one half of one of the red CCDs was out of commission during part of the project. The central fields of the LMC were observed more often and the periphery less often, as shown by the three peaks in the distribution where the first peak corresponds to the LMC periphery and the other two correspond to the center.

#### 2.3. Identifying Eclipsing Binary Stars in the MACHO Database

This section describes the techniques employed to identify EBs both in the LMC and in the SMC; the results we quote are relative to the LMC. From now on we always use the term "unfolded light curve" to indicate a set of time-ordered observations and reserve the term "light curve" to indicate a set of time-ordered observations "folded" (or "phased") around a period, omitting for brevity the adjectives folded and phased; we also use the terms EB, system, and object interchangeably.

All sources in the survey were subjected to a test for variability (Cook et al. 1995), and a large number of variable sources were identified (Alcock et al. 1995, 1996a, 1996b, 1997b). This first test starts by first eliminating the 20% most extreme photometric data points; the resulting unfolded light curve is fitted to constant brightness and its  $\chi^2$ /dof is calculated. The elimination of the most extreme points is expected to reduce the influence of noise and yield a good fit for a constant source, but not for a truly variable one. We consider the source variable if the  $\chi^2$ /dof thus computed can occur by chance with probability 1% or less. Sources that were flagged for variability were tested for periodicity. Periods were found using the Supersmoother algorithm (Reimann 1994;

 TABLE 1

 Period Determination via Supersmoother

Color	Number of EBs	$P^{a} = P_{SS}^{b}$	$P^{a} = 2P_{SS}^{b}$	$P^{a} = P_{SS}/2^{b}$	Other
Red	4634	3432 (74%)	604 (13%)	103 (2%)	495 (11%)
Blue	4634	3460 (75%)	583 (13%)	108 (2%)	483 (10%)

<sup>a</sup> Real period.

<sup>b</sup> Best period found by Supersmoother.

first published by Friedman 1984). The algorithm folds the unfolded light curve around trial periods and selects those periods in which the smoothed light curve matches the data best in a statistical sense; we have selected the best 15 possible periods ranked by the smoothness of the light curve. Periods were found separately for the red and blue unfolded light curves. The period selected as the best one by the program turned out to be "correct" in 88% of the EBs for at least one band; for 10% of the EBs the second-best period turned out to be correct for at least one band, and only for <0.5% of the EBs did the procedure fail to find a good period. In these cases "correctness" was determined by direct visual inspection.

The Supersmoother program can fail in two manners when fitting EBs. First, when one eclipse (the secondary) is very shallow, Supersmoother may not recognize it and yield a period twice the correct one. Second, when the two eclipses have nearly equal depth Supersmoother may confuse the secondary and the primary eclipses, yielding a period half the correct one. The first failure happened, for one or both bands, in about 2% of EBs, whereas the second happened in about 13% of EBs. These cases are easy to correct on visual inspection. For  $\sim 100$  EBs Supersmoother gave a period which was some other multiple of the correct one for at least one band; these were fixed on visual inspection. For the remaining EBs we tried folding the light curves around the other periods selected by Supersmoother and managed to identify the correct period for most of them. In 27 cases in which there were OGLE-II counterparts we adopted OGLE periods since, although differing in some cases by less than 1% from the periods found by Supersmoother, they gave a much better light curve. We found 51 stars in which the secondary eclipse was not evident, either because it was shallow or because the light curve was noisy, but with an OGLE-II counterpart in which it was clearly visible; these stars have not been included in the catalog. The periods in the two bands differ on average by 0.02%. These results are summarized in Table 1.

The search for variable objects in the LMC gave  $\sim 207,000$  objects of which  $\sim 66,000$  were found to be periodic. To find EBs in this sample we considered a variety of properties of light curves. The techniques we employed are the following:

1. Look at the number of photometric excursions ("dips") in the light curve. An EB is expected to show two dips in an entire period corresponding to the two eclipses, as opposed to a Cepheid or an RR Lyrae star, for which only one is expected. The number of photometric excursions was calculated by Supersmoother by counting the number of times the smoothed light curve crosses the mean: we selected stars with two excursions in both bands. We additionally imposed a cut on light-curve amplitudes: calling the amplitudes of the blue and red light curves  $Ampl_V$  and  $Ampl_R$ , respectively, as computed by Supersmoother we imposed  $Ampl_V/Ampl_R < 1.2$ . This amplitude cut was imposed to help in eliminating RR Lyrae stars from the sample, since, considering a population of several thousand probable RR Lyrae stars found in the MACHO database, we found that, on

 TABLE 2

 Summary of Cuts Applied to Define the LMC Sample

Sample	Number of EBs	2 Dips	2 Dips and $\text{Ampl}_V < 1.2\text{Ampl}_R$	s5/s5d < 1.2	Decision Tree
EB	4634	3039 (66%)	2421 (52%)	3417 (74%)	3281 (71%)
All variable sources	~66000	~8000 (~12%)	~7300 (~11%)	~19600 (~30%)	~7900 (~12%)

average,  $\text{Ampl}_V/\text{Ampl}_R \sim 1.27$ ; imposing a cut  $\text{Ampl}_V/\text{Ampl}_R < 1.2$  should therefore filter out many RR Lyrae stars. In our sample just 2421 EBs (~52%) pass this cut; we then removed the amplitude cut and look at the number of photometric excursions alone we found that 3039 EBs (~66%) pass this relaxed cut.

2. Look at the ratio of number of points 5  $\sigma$  away (s5) from the median to the number of points 5  $\sigma$  below the median (s5d). This ratio is expected to be ~2 for a typical single variable star. For an EB we expect this ratio to approach ~1 as the signal-to-noise ratio in the photometry increases, as most "outlier" points are due to eclipses. We imposed a cut s5/s5d < 1.2 in both bands and found that 3417 EBs pass it (~74%), whereas for the overall variable star data set the figure is ~19,600 out of 66,000 or ~30%.

3. Use a decision tree. We applied the decision tree program described in Murthy et al. (1994), which was run on all the variable objects on the catalog and gave for each the probability that it was an EB, an RR Lyrae star, a Cepheid, a long-period variable, or an unknown object. In all,  $\sim 17,000$  objects were found most likely by the decision tree to be EBs, but only 3281 were found to be real on visual inspection and included in the sample.

4. Use a similarity technique. We finally tested the sample with a technique described in Protopapas et al. (2006) aimed at finding outliers in large data sets of variable star light curves. The technique aims at finding objects whose light curves are most dissimilar, in a statistical sense, from an "average" light curve built out of all light curves in the data set. This is accomplished by looking at all the pairs of light curves to find their mutual similarity as defined in Protopapas et al. (2006) and, for each light curve, by then combining these measures, to find its overall similarity to the rest of the sample. Light curves with a low measure of similarity are flagged as outliers. This approach was useful in finding misfolded light curves, since it found many objects for which the period for one band gave a badly folded light curve but the period for the other band gave a good folding. This happened for 198 EBs, despite these periods differing on average by just 0.18%; in this case we selected the period that gave the good light curve for both bands.

Since all the techniques we used give some false positives, each candidate was also visually inspected before inclusion in the sample; we paid closer attention to those stars which could more easily be classified as EBs without being so, like ellipsoidal variables (see  $\S$  2.6) and Cepheids and RR Lyrae stars mistakenly folded around a period twice their real one.

TABLE 3 Summary of EBs Passing More than One Cut

Cuts	No. of EBs
2 dips and s5/s5d < 1.2	2061
2 dips, $Ampl_V < 1.2Ampl_R$ , and $s5/s5d < 1.2$	1686
2 dips and decision tree	2031
s5/s5d < 1.2, and decision tree	2574
2 dips, $Ampl_V < 1.2Ampl_R$ , and decision tree	1761
2 dips, s5/s5d < 1.2, and decision tree	1488
2 dips, $Ampl_V < 1.2Ampl_R$ , $s5/s5d < 1.2$ , and decision tree	1280

These results of our search techniques are summarized in Table 2, and Table 3 shows the number of EBs that pass more than one cut. As the numbers show, these heuristic tests are far from perfect and tend to give too many candidates; however, we feel that the large dimension of our sample can allow the determination of more stringent tests, an absolute necessity for the analysis of future surveys.

Our search gave 266 objects observed in more than one field: these duplicates have different MACHO field numbers, but typically the same tile number. In this case we summed the numbers of observations in both bands for each field and chose the one which had the highest total number of observations: the object is identified by that corresponding FTS only.

Figure 2 shows a logarithmic histogram of the period distribution. Note that the periods range from a fraction of a day to several hundreds of days. Figure 3 shows a histogram of the distribution of median V, R, and V - R. Note that the magnitudes range in values from ~20 to ~14 mag both in V and R, with a peak around 18 mag.

The average photometric error for the LMC is  $\sim 0.05$  mag in both instrumental bands; the average error for a light curve as a function of median relative magnitude is in standard magnitudes is shown in Figure 4.

#### 2.4. The rms of Residuals for the LMC Sample

For the LMC sample we estimated the distribution the rms of the residuals  $O_i - C_i$  of the observations around a theoretical light curve as a function of median relative magnitude, where  $O_i$  is the

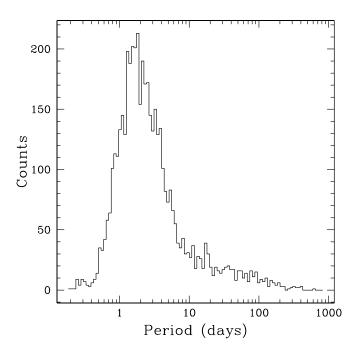


FIG. 2.—Period histogram for 4634 EBs in the LMC sample. The distribution peaks strongly in the 0.8-4 day range and has a tail in the 10-100 day range. The size of the bins is ~1/100 of the span of the logarithms of the periods.

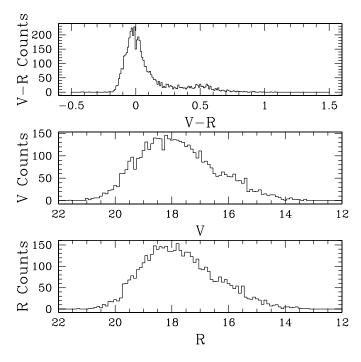


FIG. 3.—Standard V and R magnitudes and V - R histograms for the LMC sample. The bin size is 0.1 mag for the V and R histograms and 0.01 mag for the V - R one. The V - R histogram is strongly peaked around  $V - R \sim 0$  mag, showing a majority of unevolved EBs, but the longer tail, with the smaller bump around  $V - R \sim 0.5$  mag, shows a sizeable minority of fairly evolved systems, as is also shown by the higher V histogram values around 16 mag with respect to the R histogram.

value of the observed magnitude orbital phase  $\phi_i$  and  $C_i$  is the theoretical value at the same phase. Theoretical values were obtained by fitting the light curves using the JKTEBOP<sup>8</sup> code (Southworth et al. 2004a, 2004b). The JKTEBOP code is based on the EBOP code (Etzel 1981; Popper & Etzel 1981), which implements the model by Nelson & Davis (1972) with some mod-

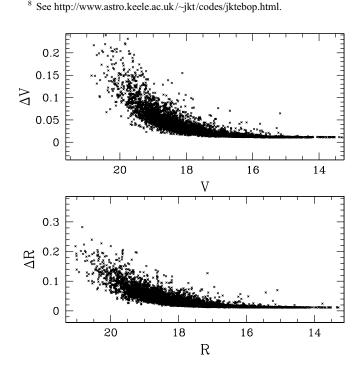


FIG. 4.—Errors as a function of median magnitude for the LMC sample.

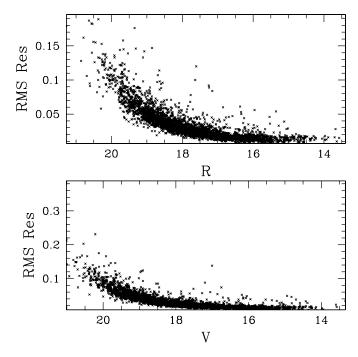


FIG. 5.—The rms of residuals as a function of median relative magnitude for the LMC sample.

ifications; JKTEBOP in turn adds several modifications and extensions to the original EBOP code that make it easier to use, especially when fitting a large number of light curves. Before fitting we eliminated outlying points by taking averages of all points in boxes containing from  $\sim 10$  to  $\sim 20$  points along a light curve and discarding the points more than  $2\sigma$  away from these averages. We obtained starting values for the model parameters by running the DEBiL code (Devor 2005) and using the values it computed; the limb-darkening values for the V and R bands were taken from (Cox 2000). We fixed the ratio of the masses, q, to 1, 0.1, and 10 and did the fit in each case taking in the end the best result. Finally, we selected light curves with  $\chi^2/dof < 2$  to show in Figure 5. Out of 4636 EBs in the LMC the program converged in 4090 cases in the *R* band and in 4312 cases in the *V* band; we found 3067 fits with  $\chi^2/dof < 2$  in the *R* band and 3198 in the *V* band. We point out that those fits were made only with the aim of obtaining a good theoretical light curve for as many observed light curves as possible in a fast and automated manner, so that a residuals distribution could be calculated. In particular, we did not attempt to accurately determine astrophysical parameters for our EBs. This is also the reason why we discarded points at just  $2\sigma$  away from the moving averages, which could result in eliminating potentially interesting information for some EBs; such objects are obviously deserving of more in depth study which we did not attempt here. While in general our fits were good in the case of largely separated, undistorted systems, they were often bad for close, strongly distorted ones, which is to be expected since JKTEBOP is not meant to be used for such systems; also, in several cases our fits were bad because the scatter of the observed values was larger than the observational errors, which suggests that other physical phenomena, such as pulsation of one or both components, are present. The rms distributions of the residuals versus median magnitudes V and R are shown in Figure 5.

### 2.5. Examples of Light Curves

Figures 6-11 show some examples of light curves. The panels on the left show the original light curves, and those on the right

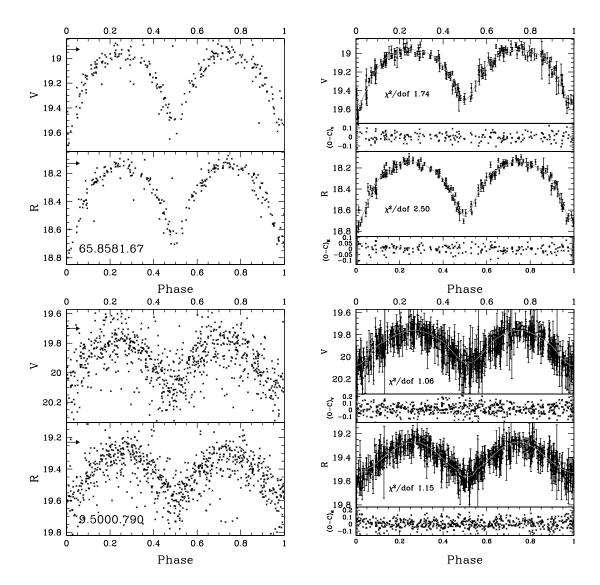


FIG. 6.—Examples of LMC EBs' light curves, arranged by ascending period. For basic data see Table 4. *Left*: Observed light curves with all data points. The arrows show the baseline as defined in Table 4. *Right*: Observed light curves with outlying points removed, theoretical light curves from the fit, and residuals.

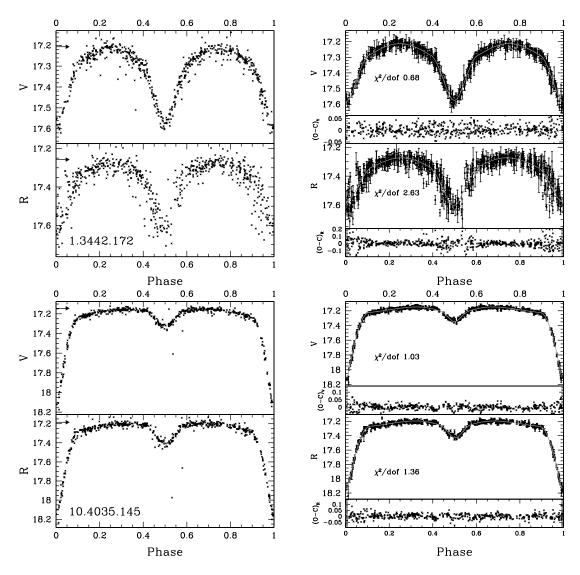


FIG. 7.—Same as Fig. 6.

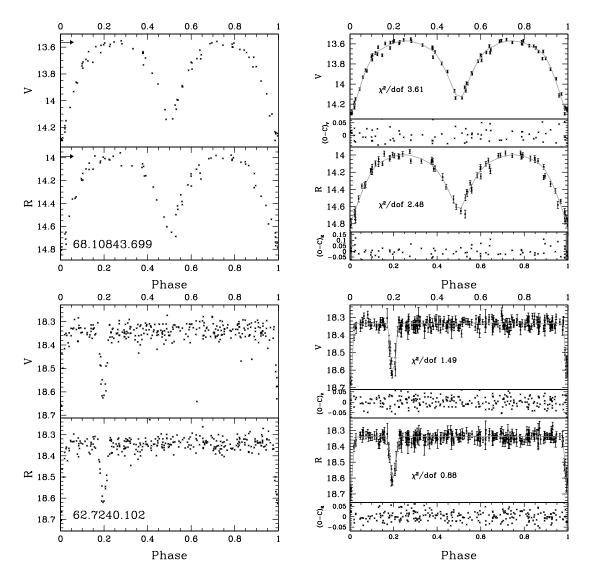


FIG. 8.—Same as Fig. 6.

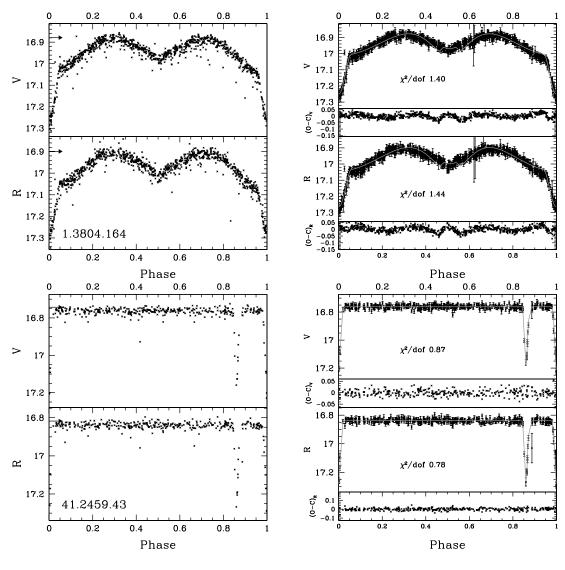


FIG. 9.—Same as Fig. 6.

show the light curves with the outlying points removed, the error bars, the theoretical light curves from the fit, and the residuals. The EBs shown are meant to be representative of the sample; this is why some examples of bad fits are included. Comparing the panels on the left with the panels on the right for these figures gives an idea of the effect of removing outlying points. In particular, the figures suggest that for those objects with good fits the procedure resulted in the elimination of truly outlying points; these EBs are mostly detached with undistorted components. For objects with bad fits, which mostly comprise EBs with close and strongly distorted components, the situation is less clear. For example, the system labeled 1.3442.172 shown in Figure 7 exhibits some points in the *R* band, at secondary eclipse around phase  $\sim 0.4$ , that run almost parallel to the main light curve but at a higher magnitude. Such points may or may not be physically significant; some of these are removed by our procedure, but the fit is nevertheless bad. The systems labeled 1.3804.164 in Figure 9 and 1.4055.98 in Figure 10 show a large and steplike scatter band, the reason for which is, we think, the intrinsic variability of the secondary component,<sup>9</sup> as suggested by the fact that the band becomes much narrower at primary eclipse but not at secondary eclipse; this interpretation is also suggested by the fact that the residuals show an oscillating behavior as a function of phase. In both 1.4055.98 and 36.5943.658 in Figure 11 the scatter band is much larger than the observational error, which explains their bad fits. These examples show that the samples contain many EBs which could be deserving of more careful study, which we did not attempt here. The properties of these EBs are summarized in Table 4; of the 12 EBs shown, 8 have two photometric excursions in both bands and  $\text{Ampl}_V/\text{Ampl}_R < 1.2$ , 7 are found by the decision tree, 5 have s5/s5d < 1.2, and 2 have a counterpart in the OGLE-II sample: 1.3442.172 (counterpart OGLE 050149.20–691945.5 in field LMC SC15) and 1.4055.98 (counterpart OGLE 050542.06– 684732.8 in field LMC SC13).

## 2.6. Ellipsoidal Variables in the Samples

Ellipsoidal variability occurs in a close binary system when one (or both) component(s) is (are) tidally distorted by the companion. If the binary system is detached, as most systems in our samples are, the distorted stars assume the asymmetric, egglike shape of the Roche equipotential surface, whereas in the case of contact system the shape of the common equipotential surface is more reminiscent of a dumbbell. The light curve of an ellipsoidal variable system reveals a continuously varying profile, with two

<sup>&</sup>lt;sup>9</sup> The component eclipsed at primary eclipse.

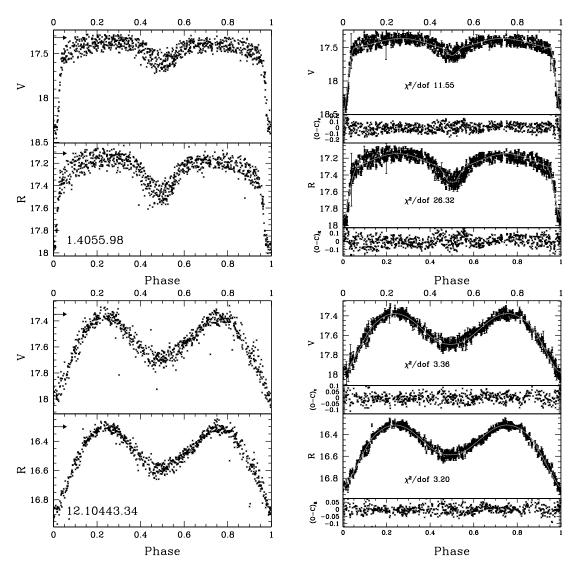


FIG. 10.—Same as Fig. 6.

maxima and two minima per period, with the minima often having different depth, whereas the maxima are usually equal. The main reason for this variability is that, as the stars rotate, their projected areas on the sky vary, reaching a maximum at the two quadratures and a minimum at the two conjunctions; the measured flux thus varies in the same way during a period. More information on ellipsoidal variables can be found in Hilditch (2001). A large sample of ellipsoidal variables in the LMC has been released by the OGLE collaboration (Soszyński et al. 2004); an analysis of ellipsoidal variables found in the MACHO database has been published by Derekas et al. (2006). A binary system can present both eclipses and ellipsoidal variability, but in many cases it may not be possible to clearly recognize an eclipse from visual inspection; this poses a problem for the compilation of EB catalogs, since the light curves of EBs and noneclipsing ellipsoidal variables can be easily confused.

We looked for possible contamination by ellipsoidal variables in our sample and found  $\sim 120$  systems exhibiting ellipsoidal variability which we then visually checked more carefully than other stars which were clearly EBs. We also attempted a less subjective approach by fitting these systems with the EBOP program (Etzel 1981; Popper & Etzel 1981; Nelson & Davis 1972) following the prescriptions of Alcock et al. (1997a); however, since EBOP is not designed for analyzing such distorted systems the final decision about whether or not to include a star exhibiting ellipsoidal variability in the sample was taken on visual inspection. Figure 12 shows two examples of EB systems with pronounced ellipsoidal variability; basic data on these systems are given in Table 5.

## 2.7. The Small Magellanic Cloud Sample

The SMC sample comprises 1509 EBs selected via the same techniques as the LMC EBs and confirmed by visual inspection; the general considerations of the preceding subsection regarding the search for variability apply here as well. The sky coverage in the SMC corresponds to MACHO fields 206, 207, 208, 211, 212, and 213; field center coordinates for these fields are given in Table 6.

Magnitudes quoted for the SMC have been obtained by using transformations which differ slightly in the zero point from the LMC ones due to the larger exposure times in the SMC (Alcock et al. 1999); they are reported in equation (2):

$$V = V_{\text{MACHO}} + 24.97 \text{ mag} - 0.18(V_{\text{MACHO}} - R_{\text{MACHO}}),$$
  

$$R = R_{\text{MACHO}} + 24.73 \text{ mag} + 0.18(V_{\text{MACHO}} - R_{\text{MACHO}}).$$
 (2)

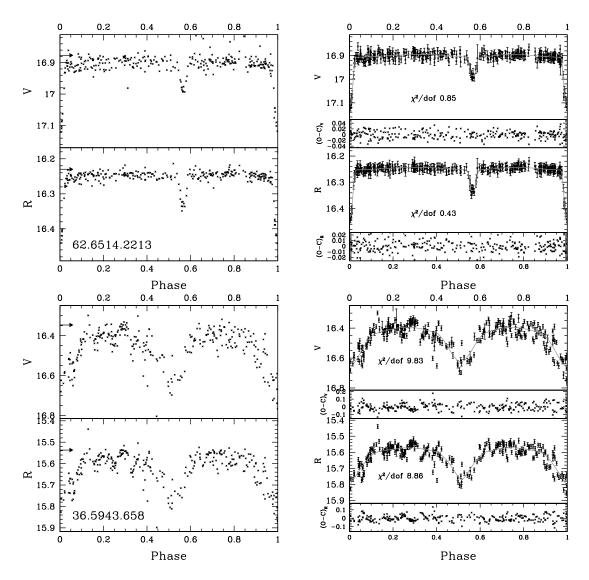


FIG. 11.—Same as Fig. 6.

TABLE 4 Basic Data for the LMC EBs Shown in Figures 6, 7, and 8  $\,$ 

MACHO ID	R.A. (J2000.0)	Decl. (J2000.0)	Period <sup>a</sup> (days)	V Baseline <sup>b, c</sup>	<i>R</i> Baseline <sup>b, c</sup>	$V - R^{c, d}$	Comment
65.8581.67	05 33 09.458	-65 30 29.13	0.19	18.93	18.13	0.8	Shortest period in sample
9.5000.790	05 11 20.548	$-70\ 21\ 00.16$	0.24	19.70	19.23	0.47	Very short period
1.3442.172	05 01 49.005	-69 19 45.60	1.02	17.21	17.26	-0.05	Fairly typical EB
10.4035.145	05 05 02.233	$-70\ 06\ 13.27$	2.53	17.14	17.19	-0.05	Fairly typical EB
68.10843.699	05 47 10.738	$-67\ 58\ 55.74$	3.07	13.56	13.99	-0.43	Bluest in sample
62.7240.102	05 24 55.090	-66 11 55.28	4.17	18.30	18.30	0.00	Very high eccentric orbit
1.3804.164	05 03 36.536	$-69\ 23\ 32.27$	4.19	16.88	16.90	-0.02	Algol type
41.2459.43	04 55 43.321	$-70\ 18\ 00.44$	13.18	16.74	16.82	-0.08	Highest eccentric orbit
1.4055.98	05 05 42.201	-68 47 33.44	24.51	17.32	17.11	0.21	Fairly typical EB
12.10443.34	05 44 47.185	$-70\ 27\ 26.65$	319.37	17.35	16.30	1.05	Reddest in sample
62.6514.2213	05 20 32.499	-66 13 17.92	417.60	16.88	16.23	0.65	Long period
36.5943.658	05 17 15.478	-71 57 45.69	633.70	16.35	15.54	0.81	Longest period in sample

NOTES.—The information in Table 4 is also available in the electronic edition of the *Astronomical Journal*. A portion is shown here for guidance regarding its form and content. The EBs are arranged by ascending period. Units of right ascension are hours, minutes, and seconds, and units of declination are degrees, arcminutes, and arcseconds. <sup>a</sup> Supersmoother provides different periods for the V and R unfolded light curves, but their difference is usually smaller than the precision to which we report their

values in this table. Online summary tables provide both periods to 5 significant digits. <sup>b</sup> The baseline is calculated in the following way. First the outlying points are eliminated by dividing the light curve in boxes of  $\sim$ 50 data points and eliminating the points which are more than 2  $\sigma$  away from the median of the 10% more huminous points is taken. This value is not the median of the

the points which are more than  $2\sigma$  away from the mean in each box. Then the median of the 10% most luminous points is taken. This value is not the median of the whole light curve that is shown in the figures.

<sup>c</sup> Values are quoted to the hundredths of magnitude, typical of MACHO observational uncertainties.

<sup>d</sup> This is the difference of the two baselines as defined above, not of the two medians as is the V - R shown in the figures. This column is not directly available in the online table but can be deduced by subtracting col. (12) from col. (10).

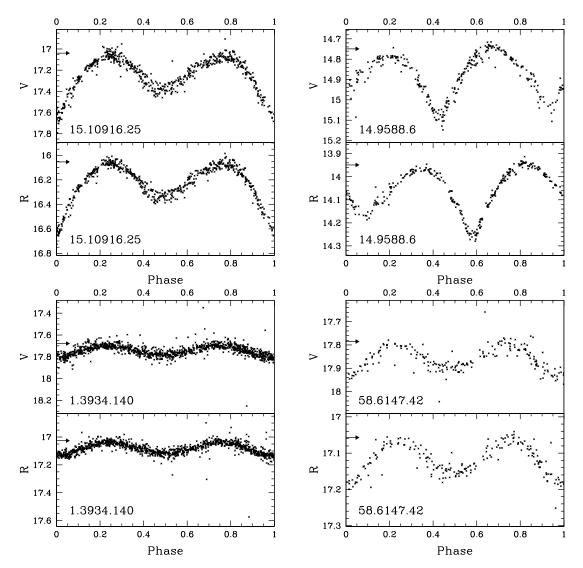


Fig. 12.—Top: Light curves for two long-period EBs with strong ellipsoidal variability in the LMC sample. Bottom: Light curves of two noneclipsing ellipsoidal variables.

The SMC search gave 194 duplicates and again we chose the field which had the highest total number of observations and the object is identified by that corresponding FTS only.

Figure 13 shows the histogram of the number of observations in both bands for the EBs in the sample. Figure 14 shows a logarithmic histogram of the period distribution. Figure 15 shows the histograms of the magnitudes for both bands, as well

1

as for color. Magnitudes range in values from  $\sim 19$  to  $\sim 14$  mag both in V and R bands, with a peak around 17 mag. The average photometric error for the SMC is again  $\sim 0.05$  mag in both instrumental bands; the error as a function of standard magnitude is shown in Figure 16. Figures 17–20 show some examples of light curves; their properties are summarized in Table 7. The "bump" shown by the star labeled 207.16374.39 is probably due

	TABLE	5			
BASIC DATA FOR T	THE LMC ELLIPSOIDAL	VARIABLES	Shown i	in Figure 1	2

MACHO ID	R.A. (J2000.0)	Decl. (J2000.0)	Period <sup>a</sup> (days)	V Baseline <sup>b, c</sup>	<i>R</i> Baseline <sup>b, c</sup>	$V - R^{c, d}$	Eclipsing
1.3934.140	05 04 23.977	-68 49 21.65	85.88	17.68	17.03	0.65	No
58.6147.42	05 18 03.677	-66 27 20.17	105.08	17.78	17.06	0.72	No
15.10916.25	05 47 21.831	-71 10 46.49	355.28	17.04	16.05	0.99	Yes
14.9588.6	05 39 28.498	-71  00  46.01	411.04	14.75	13.95	0.80	Yes

NOTE.—Units of right ascension are hours, minutes, and seconds, and units of declination are degrees, arcminutes, and arcseconds.

<sup>a</sup> Supersmoother provides different periods for the V and R unfolded light curves, but their difference is usually smaller than the precision to which we report their values in this table. Online summary tables provide both periods to 5 significant digits. The variables are arranged by ascending period. <sup>b</sup> See Table 4 for an explanation of the baseline calculation.

<sup>c</sup> Values are quoted to the hundredths of magnitude, typical of MACHO observational uncertainties.

<sup>d</sup> This is the difference of the two baselines, not of the two medians as is the V - R shown in the figures.

211.....

213.....

212

MACHO Field Coordinates for the SMC					
Field ID	R.A. (J2000.0)	Decl. (J2000.0)			
206	01 05 21.70	-72 26 58.3			
207	00 57 16.58	-72 34 57.0			
208	00 48 03.19	-72 34 20.9			

00 58 27.40

00 49 10.27

00 40 18.91

-73 04 55 3

-73 13 32.9

73 08 49.5

TABLE 6

Note.-Units of right ascension are hours, minutes, and seconds, and units of declination are degrees, arcminutes, and arcseconds.

to star spots: we were able to roughly reproduce it by appropriately choosing spots on the components and fitting the light curve using the PHOEBE<sup>10</sup> (Prša & Żwitter 2005) software package.

## 3. COLOR-MAGNITUDE DIAGRAM AND COLOR-PERIOD DIAGRAM

#### 3.1. The Large Magellanic Cloud Sample

Figure 21 shows the CMD for the 4634 EBs in the LMC sample; the lower magnitude limit is  $V \sim 21$  mag. We estimated the reddening by using the LMC extinction map described in the LMC photometric survey of Zaritsky et al. (2004). The extinction catalog produced by the survey is available for query online, and we retrieved the values of  $A_V$  specified in Table 8, based on the *hot* stars only found by the survey (T > 12,000 K) in a radius of 12' (the maximum allowed) around the positions specified in Table 8, which sample the EB position distribution.

From the values of Table 8 we derive a mean value for  $A_V$  of 0.64 mag, which we use to characterize the average LMC V extinction. We use the reddening vector  $A_V/E(V-R) = 5$  from

10 See http://phoebe.fiz.uni-lj.si.

<sup>11</sup> See http://ngala.as.arizona.edu/dennis/lmcext.html.

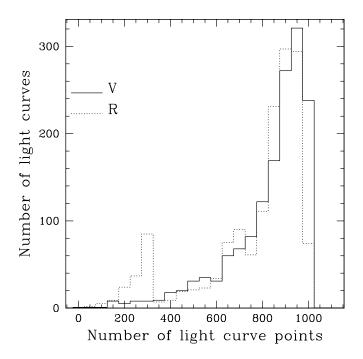


FIG. 13.—Histogram of the number of light-curve points for both bands for the SMC sample.

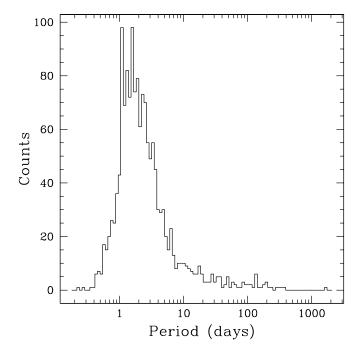


FIG. 14.—Period histogram for 1509 EBs in the SMC sample. The size of the bins is  $\sim 1/100$  of the span of the logarithms of the periods.

Alcock et al. (1997b and references therein) and find  $\langle E(V-R) \rangle =$ 0.128 mag, more than a factor of 2.5 larger than the value 0.049 mag found by Alcock et al. (1997b). This is likely due to the fact that the reddening for the EBs are likely to be along lines of sight toward young, hot stars in the Zaritsky et al. (2004) catalog which are derived to have higher  $A_V$ , while the Alcock et al. (1997b)  $A_V$  was derived from observations of RR Lyrae stars.

As the CMD shows, the sample is made up mostly of bright early-type stars: from the range in magnitudes and assuming an

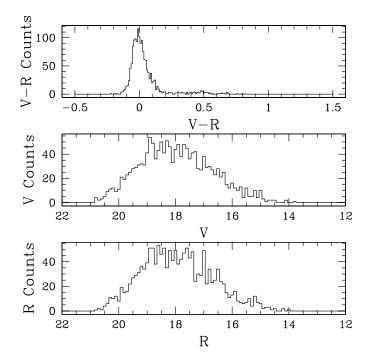


FIG. 15.—V and R magnitudes and V - R histograms for 1508 EBs in the SMC sample. The bin size is 0.1 mag for the V and R histograms and 0.01 mag for the V - R one.

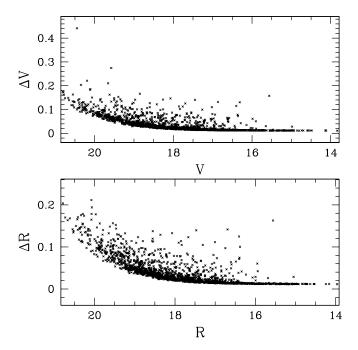


FIG. 16.—Errors as a function of median magnitude for the SMC sample.

LMC distance modulus of 18.5 mag (van der Marel et al. 2002), we see that in most cases at least one component is of spectral type B or A (Alcock et al. 2000b; Cox 2000). We employ the term "young star region" to describe the main feature on the left part of the CMD, rather than main sequence, because our sample contains some bright and short-lived stars that may not be burning hydrogen in their core, while still being on the blue part of the CMD; likewise, we employ the term "evolved star region" to indicate the feature on the red part of the CMD. We define the young star region as V - R < 0.2 mag and the evolved star region as V - R > 0.2 mag: with these definitions we find 3760 EBs in the young star region and 874 EBs in the evolved star region. We used a simple cut to separate the young star region from the evolved star region rather than a more precise one, because our cut can be easily seen both in the CMD and in the color-period diagrams. An interesting feature of the CMD is the lack of a clear gap between the young star region and the evolved star region; there is instead a fairly continuous transition, with a higher number of systems filling the Hertzsprung gap that would be expected from CMDs of single stars. This may indicate that these systems are composed of a more massive and hence more evolved and redder star and a less massive, less evolved, bluer one.

The color-period diagram is shown in Figure 22 (left); this diagram clearly shows the young EBs with periods  $P \leq 20$  days and a second population (333 objects) of long-period, evolved EBs with periods P > 20 days and V - R > 0.2 mag. Several interesting features emerge in Figure 22: there is a paucity of longperiod objects on the young star region of the CMD, and a corresponding lack of short-period objects with very red colors. Furthermore, the red (V - R > 0.2 mag) population shows a positive correlation between period and color. There are virtually no long-period, blue objects or short-period, red objects in this group. In contrast, the young star region shows no such correlation. This structure in the color-period diagram is a consequence of (1) Kepler's third law, (2) the probability that an EB is favorably oriented in space to allow eclipses to be detected [prob =  $(R_1 + R_2)/a$ , where  $R_1$  and  $R_2$  are the radii of the primary and secondary stars, respectively, and a is the semi major axis], and (3) the fact that objects usually evolve in this diagram at constant period,

from blue to red. Long-period binary stars have large semimajor axes. When both stars are on the young star region, their relatively small radii yield a relatively low probability that they will eclipse when seen from our vantage point. When one of the pair evolves away from the young star region, one of these radii (typically  $R_1$ ) will increase. The consequence of this is an increase in the probability that eclipses will be detected. This accounts for the presence of red, long-period stars and the absence of corresponding young progenitors. The situation is different for shortperiod systems. These are relatively likely to be detected because of their small semimajor axes, and are prominent on the blue side. As one of these stars evolves and expands rapidly, it may engulf the companion and enter a stage of common-envelope evolution in which the expanding star overflows the second Lagrangian point L2 Paczynski 1976), leading to the disappearance of eclipses. Common-envelope system differ from contact binaries (Kallrath & Milone 1999; Hilditch 2001; Shore et al. 1994),<sup>12</sup> in which two young stars overflow their first Lagrangian point (L1) and their Roche equipotential surface assumes a dumbbell shape. Contact systems usually show ellipsoidal variation and, if the orbital inclination is large enough, also eclipses; EBs of the W UMa type belong to this category. Shore et al. (1994) and Iben & Livio (1993) provide more information on common-envelope binaries. The correlation between period and color among red objects reflects the general correlation between radius and color for the evolved partner.

## 3.2. Foreground Objects

Figure 22 (*left*) reveals a population of  $\sim$ 63 EBs with low periods ( $P \leq 2$  days) and high color (V - R > 0.3 mag). These objects are probably foreground Galactic EBs composed of late-type stars. This interpretation is suggested by several factors. First, due to the large angular extent of the LMC, there is foreground contamination in the LMC MACHO fields (Alcock et al. 2000b); in particular, the feature marked "H" in the CMD of their Figure 1 indicates foreground Galactic disk stars and is centered at V- $R \sim 0.5$  mag, as is our presumptive foreground population. Second, both the short period of these EBs and the shape of their light curves, which are either detached or mildly distorted, strongly suggests that the stars making up this population are small, latetype stars; this is further borne out by their color, again typical of a solar-like star. Finally, the CMD of this population, shown in Figure 23, clearly shows what appears to be a turnoff feature at  $V - R \sim 0.4$  mag, with few evolved objects (V - R > 0.7 mag). It is interesting to note that the overall shape of this population in the color-period diagram shows, on a smaller scale, the same features of the LMC diagram; a main sequence<sup>13</sup> is clearly visible in Figure 23, and the evolved EBs show the same color-period correlation of their LMC counterparts in Figure 22.

### 3.3. The Small Magellanic Cloud Sample

Figure 24 shows the CMD for 1508 EBs in the SMC sample out of the 1509 in the sample; one EB which has valid data only in the  $R_{MACHO}$  band is not shown because it was not possible to determine the standard magnitudes via equation (2). The general remarks made for the LMC CMD apply here as well, and we used a reddening vector with the same inclination as the LMC. The figure clearly shows the young star region, which is composed of 1412 EBs (94%), whereas there are just 96 evolved EBs. We

<sup>&</sup>lt;sup>12</sup> Called "over contact" in Kallrath & Milone (1999).

<sup>&</sup>lt;sup>13</sup> We employ this term since these foreground stars are probably not very massive and therefore are in their core hydrogen burning phase.

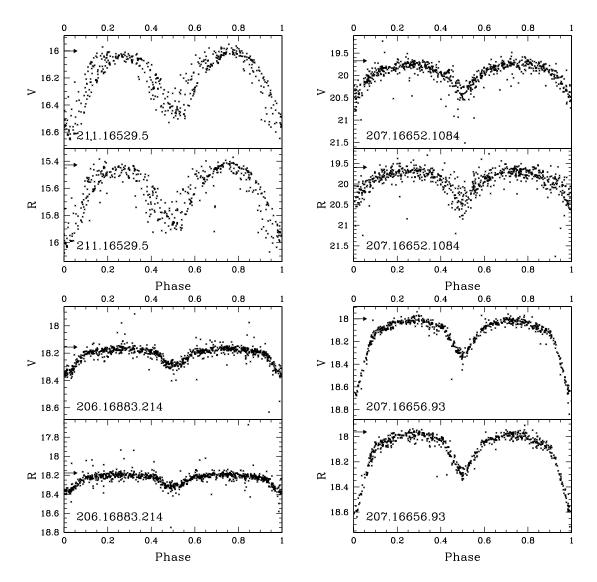


FIG. 17.—Examples of light curves of EBs in the SMC sample. For basic data, see Table 7. The arrows show the baseline as defined in Table 7. The EBs are arranged by ascending period.

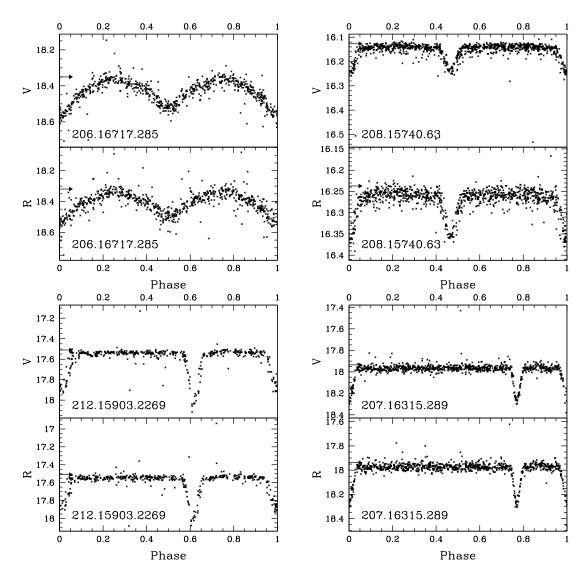


FIG. 18.—Same as Fig. 17.

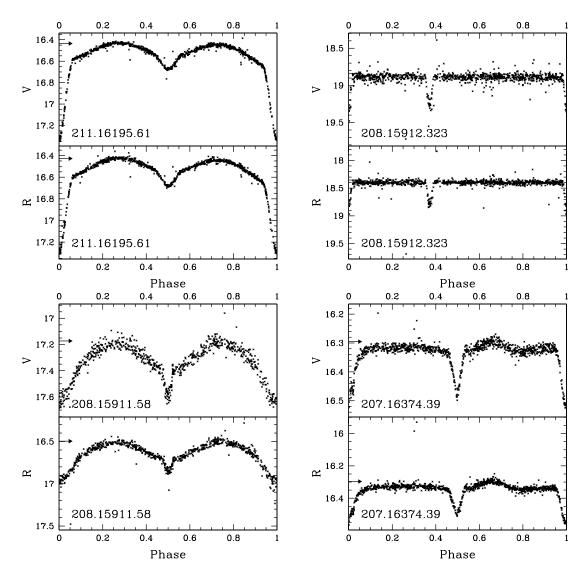


FIG. 19.—Same as Fig. 17.

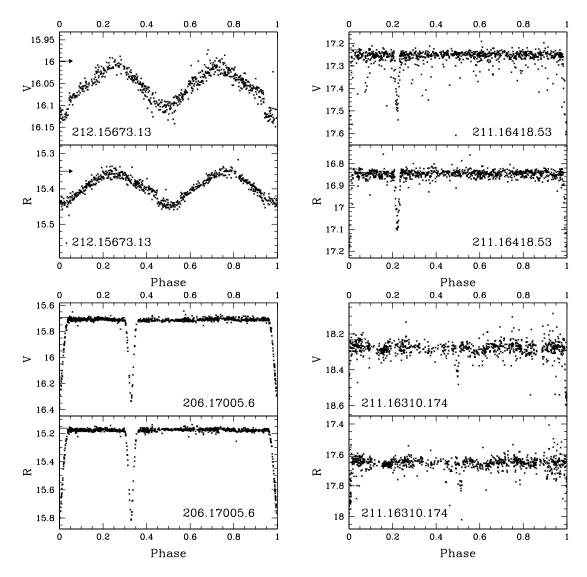


FIG. 20.—Same as Fig. 17.

TABLE 7			
BASIC DATA FOR THE SMC EBs SHOWN IN FIGURES 17, 12	8, 19,	AND	20

MACHO ID	R.A. (J2000.0)	Decl. (J2000.0)	Period <sup>a</sup> (days)	V Baseline <sup>b,c</sup>	<i>R</i> Baseline <sup>b,c</sup>	$V - R^{c,d}$	Comment
211.16529.5	00 59 31.368	-73 26 56.04	0.28	16.00	15.43	0.57	Shortest period in sample
207.16652.1084	01 00 43.656	-72 51 51.48	0.36	19.67	19.59	0.08	Very short period
206.16883.214	01 04 25.272	-72 37 48.36	1.14	18.16	18.18	-0.02	Fairly typical EB
207.16656.93	01 00 56.345	-72 36 44.40	1.23	18.00	17.96	0.04	Highly eccentric orbit
206.16717.285	01 01 41.400	-72 19 25.68	1.65	18.35	18.32	0.03	Fairly typical EB
208.15740.63	00 46 13.949	-72 52 37.03	1.74	16.13	16.24	-0.11	Bluest in sample
212.15903.2269	00 49 18.192	-73 21 55.44	2.42	17.51	17.51	0.00	Highly eccentric orbit
207.16315.289	00 55 48.168	-72 29 33.36	3.34	17.93	17.94	-0.01	Highly eccentric orbit
211.16195.61	00 53 59.729	-72 56 56.13	4.73	16.44	16.43	0.01	Fairly typical EB
208.15912.323	00 49 10.440	-72 46 37.56	120.51	18.84	18.35	0.49	Highly eccentric orbit
208.16.58	00 49 28.392	$-72\ 49\ 40.80$	137.89	17.17	16.50	0.67	Reddest in sample
207.16374.39 <sup>e</sup>	00 56 25.872	-72 22 15.96	186.34	16.30	16.30	0.00	Long period
212.15673.13	00 45 46.824	-73 31 32.52	200.27	16.00	15.35	0.65	Long period
211.16418.53	00 57 5.304	-73 15 10.44	234.64	17.23	16.82	0.41	Highly eccentric orbit
206.17005.6	01 06 10.224	$-72\ 06\ 24.48$	371.89	15.69	15.16	0.53	Highly eccentric orbit
211.16310.174	00 55 30.024	-72 52 49.44	1559.81	18.23	17.61	0.62	Longest period in sample

NOTES.—The information in Table 7 is also available in the electronic edition of the *Astronomical Journal*. A portion is shown here for guidance regarding its form and content. The EBs are arranged by ascending period. Units of right ascension are hours, minutes, and seconds, and units of declination are degrees, arcminutes, and arcseconds. <sup>a</sup> Supersmoother provides different periods for *V* and *R* unfolded light curves, but their difference is usually smaller than the precision to which we report their values

in this table. Online summary tables provide both periods to 5 significant digits. <sup>b</sup> The baseline is calculated in the following way. First, outlying points have been eliminated by dividing the light curve in boxes of  $\sim$ 50 data points and eliminating the points which were more than 2  $\sigma$  away from the mean in each box. Then the median of the 10% most luminous points was taken. This value is not the median of the

whole light curve that is shown in the figures.

<sup>c</sup> Values are quoted to the hundredths of magnitude, typical of MACHO observational uncertainties.

<sup>d</sup> This is the difference of the two baselines as defined above, not of the two medians as is the V - R shown in the figures. This column is not directly available in the online table but can be deduced by subtracting col. (12) from col. (10)

<sup>e</sup> There is a curious "bump" in the light curve of this long-period EB (Figure 19) that suggests further investigation.

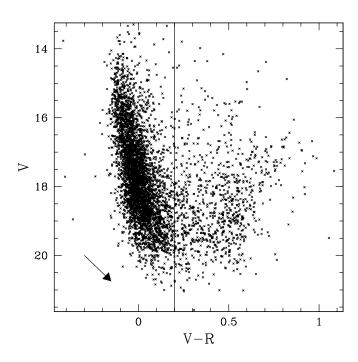


FIG. 21.—CMD for 4634 EBs in the LMC sample. The sample is made up mostly by young luminous stars (with at least one component of spectral type B or A). A fairly high number of EBs (~19%) are evolved; there are no real "gaps" between the young star region and the evolved star region. The vertical line shows the cut used to separate the young star region from the evolved star one. The reddening vector is  $A_V/E(V - R) = 5$ ; the adopted values of  $\langle A_V \rangle$  and  $\langle E(V - R) \rangle$  are 0.64 and 0.128 mag.

estimate the SMC reddening from Zaritsky et al. (2002); from their Figure 19 we infer a mean  $A_V \sim 0.3$  mag for their hotter SMC population, relevant to our sample, which is composed mostly of early-type hot stars in the young star region. We use the same reddening vector as the LMC,  $A_V/E(V-R) = 5$ , and find a mean E(V-R) = 0.06 mag.

The color-period diagram is shown in Figure 22 (*right*); the general considerations made for the LMC color-period diagram apply here as well. The diagram shows five EBs with low period (P < 1 days) and red color ( $V - R \sim 0.6$  mag) which are probably foreground objects. The much smaller number of foreground objects in the SMC is probably due both to its smaller angular

TABLE 8

Extinctio	N VALUES IN THE LMC	
R.A. (J2000.0)	Decl. (J2000.0)	$A_V$
06 06 00	-69 05 00	0.48
06 06 00	$-72\ 43\ 00$	0.97
05 40 00	-65 30 00	0.75
05 40 00	$-69\ 05\ 00$	0.80
05 40 00	-72  30  00	0.78
05 20 00	-65 30 00	0.53
05 20 00	$-69\ 05\ 00$	0.50
05 20 00	-72  30  00	0.56
05 00 00	-65 30 00	0.50
05 00 00	$-69\ 05\ 00$	0.46
05 00 00	$-72\ 43\ 00$	0.45
04 40 00	$-69\ 05\ 00$	0.62
04 40 00	-72  30  00	0.97

Note.—Units of right ascension are hours, minutes, and seconds, and units of declination are degrees, arcminutes, and arcseconds.

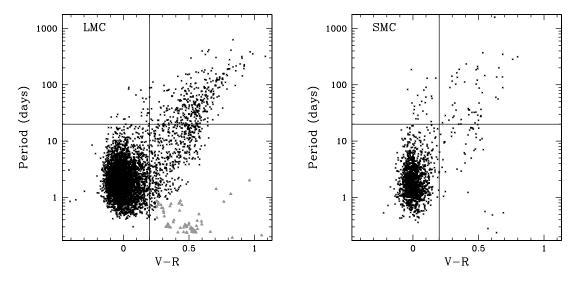


FIG. 22.—Left: Color-period diagram for 4634 EBs in the LMC. The gray triangles represent the foreground population. Right: Color-period diagram for 1508 EBs in the SMC. The figure shows that the fraction of long-period EBs that belong to the young star region in the SMC is higher than in the LMC.

size and to its higher Galactic latitude ( $l \sim -44^{\circ}$  compared to  $l \sim -33^{\circ}$  for the LMC). We can further test the hypothesis that these two short-period, red populations in the LMC and SMC are due to foreground objects by comparing the ratio of their numbers to the ratio of the areas of the LMC and SMC, which we can estimate from Figures 28 and 37; if these objects are indeed fore-ground, these two ratios should be roughly equal. From the figures we can estimate the sky area of the LMC as ~110 deg<sup>2</sup>, and the sky area of the SMC as ~10 deg<sup>2</sup>; their ratio is thus similar to the ratio of the numbers of EBs in the two populations as expected.

## 4. COMPARISON BETWEEN THE LMC AND THE SMC SAMPLES

Although the basic features of the CMD and the color-period diagram are the same for LMC and SMC, there are some differences, shown by Figure 22 and Table 9.

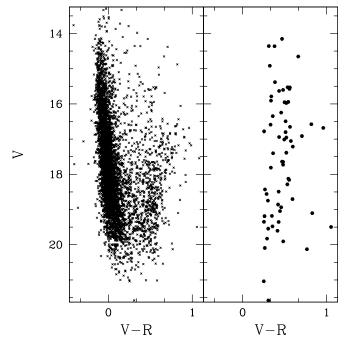


Fig. 23.—CMD of the LMC sample (*left*) and of the foreground population (*right*).

The fraction of blue (V - R < 0.2 mag) EBs is higher in the SMC than in the LMC. More striking, the fraction of blue, longperiod (V - R < -0.2 mag, P > 20 days) EBs is much higher in the SMC than in the LMC.

To further investigate the differences between the two samples we carried out a Kolmogorov-Smirnov (K-S) test on the distributions of the absolute magnitudes  $M_V$  and  $M_R$ , their difference  $M_V - M_R$ , and the periods P of the two samples. We adopted a distance modulus of of 18.88 for the SMC (Dolphin et al. 2001) and 18.5 for the LMC (van der Marel et al. 2002). Magnitudes and colors were dereddened using  $\langle A_V \rangle = 0.64$  mag,  $\langle E(V - R) \rangle =$ 0.128 mag for the LMC and  $\langle A_V \rangle = 0.3$  mag,  $\langle E(V - R) \rangle =$ 0.06 mag for the SMC before subtracting the distance moduli. The empirical cumulative distribution functions (ECDFs) of these quantities are shown in Figure 25.

A K-S test confirms that the distributions of P and  $M_V - M_R$ are different at >99.9% confidence level; for the distributions of

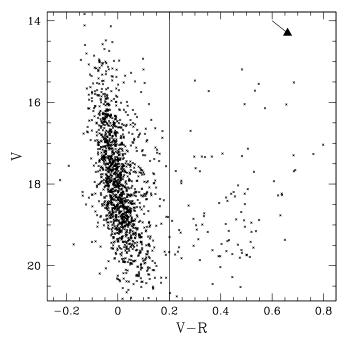


FIG. 24.—CMD for 1508 EBs in the SMC sample. The reddening vector is  $A_V/E(V-R) = 5$ ; the adopted values of  $\langle A_V \rangle$  and  $\langle E(V-R) \rangle$  are 0.3 and 0.06 mag.

## ECLIPSING BINARY STARS FROM MACHO

TABLE 9
Summary of Long-Period EBs in the SMC and LMC $% \mathcal{A}$

Galaxy	Total	Young Stars <sup>a</sup>	Evolved <sup>b</sup>	Long Period <sup>c</sup>	Long-Period Young Stars <sup>a,c</sup>	Long-Period Evolved Stars <sup>b,c</sup>
LMC	4634	3760 (81%)	874 (19%)	356	23 (6%)	333 (94%)
SMC	1508	1412 (94%) <sup>d</sup>	96 (6%) <sup>d</sup>	75	23 (31%)	52 (69%)

<sup>a</sup> Defined as V - R < 0.2 mag.

<sup>b</sup> Defined as V - R > 0.2 mag.

<sup>c</sup> Defined as P > 20 days.

<sup>d</sup> One SMC EB has no valid  $V_{MACHO}$  data; hence, the sum of the young star and evolved star numbers for the SMC is 1508.

 $M_V$  and  $M_R$  the K-S test gives a probability of ~99.4% and ~98.5% for them being different, respectively.

# 5. CROSS-CORRELATION WITH THE OGLE-II SAMPLES

The  $M_V - M_R$  plot shows that EBs in the SMC tend to be bluer, not surprising given that a higher percentage of objects belong to the young star CMD region in the SMC than in the LMC. The period distributions show that the SMC EBs have on average shorter periods, again not surprising given the much higher percentage of evolved systems in the LMC than in the SMC and the fact that evolved systems have on average higher periods than the young systems (as shown by the color-period diagrams in Fig. 22). The EBs in our samples have been cross-correlated with the corresponding OGLE-II samples. Stars in the samples were identified if their right ascension and declination differed by less than 27.2" and their periods differed by <1%. We used a very large search radius to be conservative. The astrometric precision for both surveys is typically  $\sim 1$ ", but a few stars which had much larger differences in right ascension and/or declination turned out to be matches on inspection of their periods: in particular, we found in the LMC 32 matches with a position difference bigger than 10" and

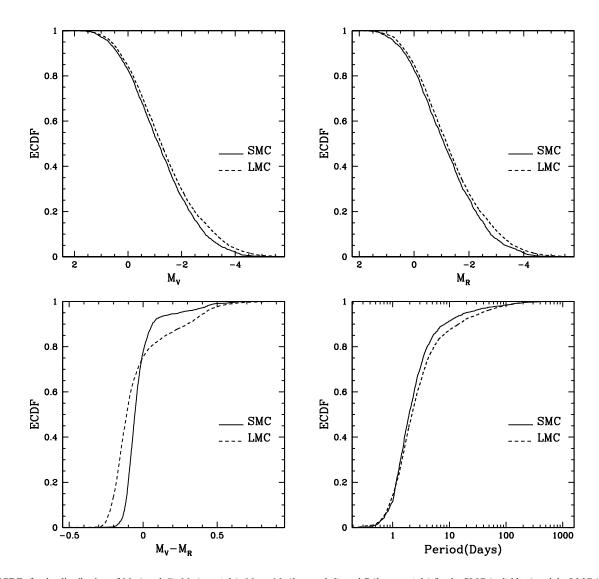


Fig. 25.—ECDFs for the distribution of  $M_V$  (top left),  $M_R$  (top right),  $M_V - M_R$  (bottom left), and P (bottom right) for the SMC (solid line) and the LMC (dashed line).

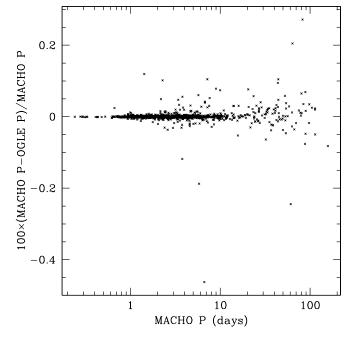


Fig. 26.—Percentage difference for MACHO vs. OGLE-II period for the 1236 OGLE-II matches in the LMC sample.

2 matches with a position difference bigger than 20". However, most of the matches were within narrower radii: for the LMC roughly half of the matches (534 out of 1236) were found within  $\sim 2^{''}$ , compatible with the astrometric precision of both the MACHO and OGLE surveys; almost all of them (1019) were within  $\sim 4''$ . We tested the robustness of our method of finding matches by investigating the probability for two periodic objects with a period difference of <1% to be within 27.2" of each other. To do this we selected a random sample of 5000 objects out of the  $\sim$ 66,000 periodic ones found by MACHO in the LMC and we counted the frequency of pairs of objects with both periods from the red and the blue light curves (as found by Supersmoother) differing by <1% and positions within 27.2". Most of the matches we found were due to the same object being observed in different tiles, and only in one case did we find a possibly genuine match; we thus conclude that the probability of two objects being erroneously classified as a match is  $\sim 0.02\%$ , and therefore our method of finding matches is robust.

#### 5.1. The Large Magellanic Cloud Sample

Our search produced 1236 matches in the LMC. The MACHO and OGLE-II periods agree to high accuracy, as shown in Figure 26—usually much better than the 1% cut we imposed. Histograms of position differences are shown by Figure 27. Both panels show the entire span of the differences; the differences in right ascension range from approximately -20'' to approximately +20'', but the left panel shows this range multiplied by the cosine of the declination (approximately  $-70^{\circ}$ ), which gives a range from approximately -7'' to approximately +6''.

The sky coverage of the two surveys was different: OGLE-II, from which the sample was derived, covered about 4.5 deg<sup>2</sup> in the central region of the LMC, whereas the sky coverage of MACHO was larger. Figure 28 shows the positions of the EBs in both catalogs, and Figure 29 shows the corresponding MACHO field number; the fields at the center of the LMC are drawn with continuous lines, those at the periphery with dashed lines.

### 5.2. Comparison between the Center and the Periphery of the LMC

In view of the different sky coverage of the MACHO and OGLE-II surveys, it is interesting to analyze separately the stars in MACHO fields covering the center of the LMC (which roughly correspond to the OGLE-II sky coverage) and the stars in the MACHO fields at the periphery. Figure 29 shows that the fields in the center are 1, 2, 3, 5, 6, 7, 8, 10, 11, 12, 13, 14, 15, 18, 19, 47, 77, 78, 79, 80, 81, and 82. There are 2620 EBs in the center and 2014 in the periphery. Figure 30 shows the CMD and the color-period diagram for the center and the periphery of the LMC, respectively; Figure 31 shows the histograms for the magnitudes, the color, and the period. The figures reveal several differences between the two samples; to check these we performed a K-S test for V, V - R, and P and found that at a high confidence level (>99.9%) the distributions are different. These differences are statistically significant but not large enough to be considered astrophysically important. In particular, the difference in period distribution could be attributed to the lower sampling in the outer fields, making it less likely to detect the longer period EBs. The

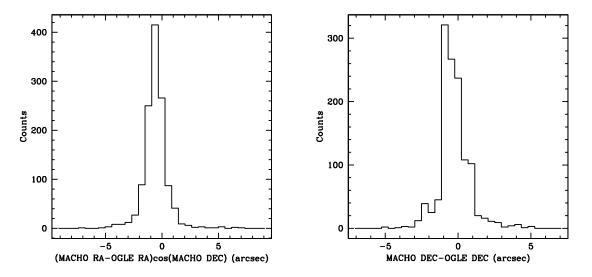


FIG. 27.—Left: Histogram of the differences between right ascensions for 1236 MACHO OGLE-II matches in the LMC. Right: Histogram of the differences between declinations. The bin size is equal to 1/30 of the range of the differences in both cases.

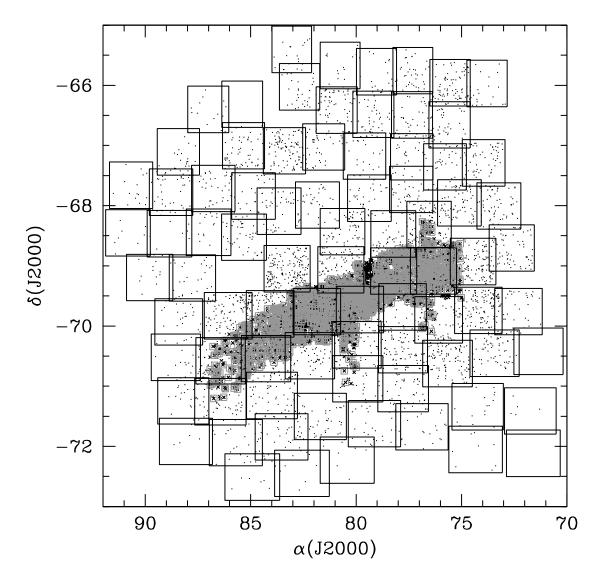


Fig. 28.—Cross-correlation between MACHO and OGLE-II LMC samples. Dots represent MACHO stars, crosses OGLE stars, and gray open boxes the matches.

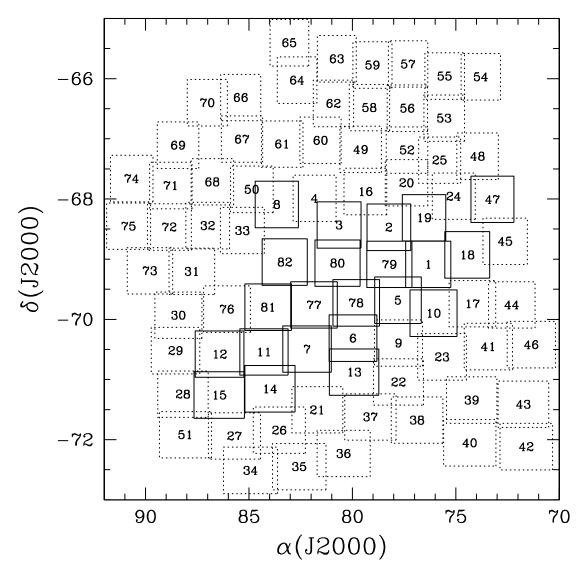


FIG. 29.—MACHO LMC field numbers.

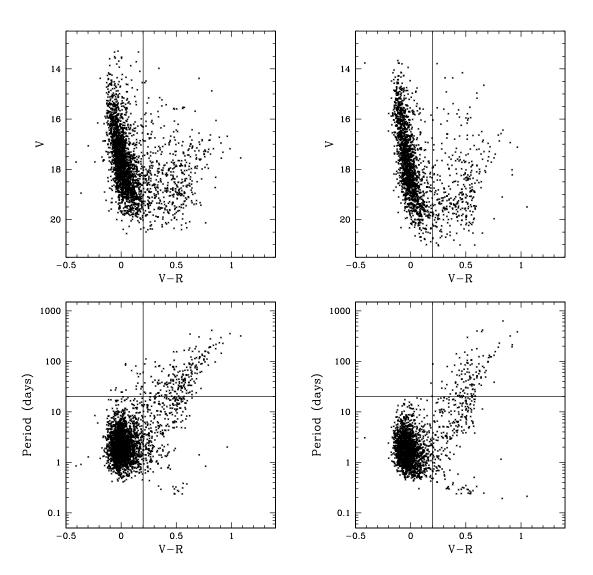


Fig. 30.—*Top left*: CMD for 2620 EBs in the center of the LMC. *Top right*: CMD for 2014 EBs at the periphery of the LMC. The CMDs suggest a more continuous transition from the young star region to the evolved star region in the center than in the periphery, especially for V < 19 mag. *Bottom panels*: Color-period diagrams for the same populations. *Bottom left*: Center. *Bottom right*: Periphery. The color-period diagrams reveal the presence of a long-period (20–100 days), relatively unevolved ( $V - R \sim 0.2$  mag) population in the center but not in the periphery.

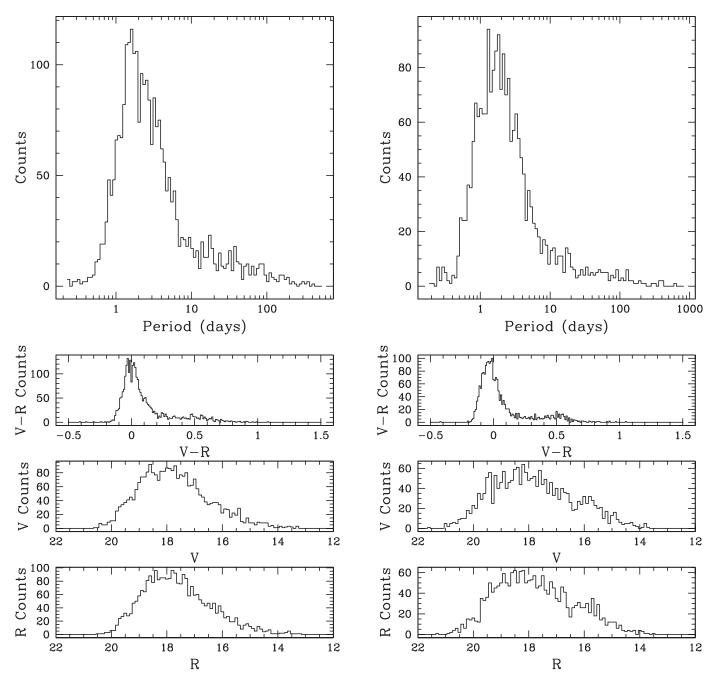


Fig. 31.—*Top left*: Period histogram for 2620 EBs in the center of the LMC. *Top right*: Period histogram for 2014 EBs at the periphery of the LMC. The size of the bins is  $\sim 1/100$  of the span of the logarithms of the periods. *Bottom panels*: Magnitude and color histograms. *Bottom left*: Center. *Bottom right*: Periphery. The bin size is 0.1 mag for the V and R histograms and 0.01 mag for the V – R one.

sampling might also be the cause of the periphery having a higher percentage of bright EBs, since these are easier to find with fewer epochs.

## 5.3. Discussion of the OGLE-II—MACHO Comparison

We finally investigated why we did not find more matches with OGLE-II. The most important reason, we think, is the fact that the techniques employed in assembling the samples are different: the OGLE team built their samples via neural networks (Wyrzykowski et al. 2003, 2004). The two surveys have roughly comparable limiting magnitudes,  $V \sim 21.5$  mag; nevertheless, we checked how the performance of the two surveys varied with magnitude. We compared the distribution of the V magnitudes for the 2620 EBs in the central region of the LMC in our sample with those of

1198 matches and the 1327 EBs from OGLE-II without MACHO counterparts (these two numbers do not add up to 2580, the size of the OGLE-II sample, because for some EBs the *V* magnitude was not reported). The histograms of these three distributions are shown in Figure 32.

The figure shows that OGLE-II EBs with MACHO counterparts, peaking at  $V \sim 18$  mag like the MACHO sample, are on average brighter than those without MACHO counterparts, which peak at  $V \sim 19.5$  mag. The shape of the V distribution of OGLE-II EBs with MACHO counterparts much more closely resembles the MACHO V distribution; a K-S test gives a probability of the two distributions being the same of ~46%. The distributions of MACHO V and OGLE-II V without MACHO counterparts, as well as those of these two OGLE-II populations, are, on the other

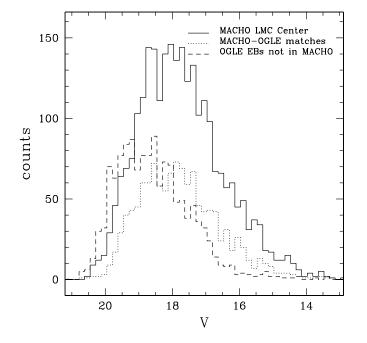


FIG. 32.—V distribution for 2620 MACHO EBs in the central region of the LMC (*solid line*), 1198 OGLE-II MACHO matches (*dotted line*), and 1327 OGLE-II EBs without MACHO counterparts (*dashed line*). The figure shows that OGLE-II EBs with MACHO counterparts are on average brighter than those without, and the shape of their V distribution more closely resembles the MACHO V distribution. This is confirmed by a K-S test.

hand, shown to be different at a >99.9% confidence level. Both distributions vanish at  $V \sim 20.5$  mag, showing that their limiting magnitudes are comparable.

We then studied the distributions of the periods: Figure 33 shows that the OGLE-II EBs without MACHO counterparts have on average longer periods than MACHO EBs in the center of the LMC and than OGLE-II EBs with a MACHO counterpart, and the difference is statistically significant in both cases; the period distributions of the MACHO EB of the LMC center and of the MACHO OGLE-II matches are statistically different as well. Therefore, OGLE-II finds a higher proportion of fainter objects than MACHO, and this does play a role in not finding a higher number of OGLE-II counterparts to our sample.

We finally studied the distribution of the MACHO-OGLE matches as a function of V. We first counted the number of OGLE-II LMC EBs in the MACHO fields, finding 2517 of them, out of a total of 2580; of these 2517 EBs, 1236 were the matches described above and 1281 did not have a MACHO counterpart (this last number is smaller than 1327, the total number of OGLE EBs without MACHO counterpart, because we are now only considering OGLE EBs in MACHO fields). We then studied the distribution, as a function of V, of the OGLE EBs in the MACHO fields that both had and did not have a MACHO counterpart and for which the V magnitude was reported: there were 1198 of the former and 1267 of the latter. We finally performed the inverse calculation, by first counting the number of MACHO LMC EBs in the OGLE-II fields and finding 1551 of them; of these 1225 had an OGLE-II counterpart and 326 did not; we studied the distribution of both these populations as a function of V. The OGLE-II field boundaries were estimated by taking the coordinates of the most extreme EBs in each OGLE-II field. These findings are summarized in Table 10.

The distributions of both the OGLE-II EBs with MACHO counterpart and of the MACHO EBs with OGLE-II counterparts

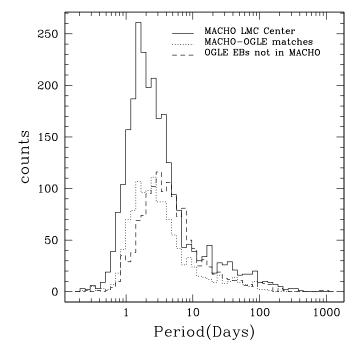


FIG. 33.—Period distribution for 2620 MACHO EBs in the central region of the LMC (*solid line*), 1198 OGLE-MACHO matches (*dotted line*), and 1327 OGLE-II EBs without MACHO counterparts (*dashed line*). The figure shows that OGLE-II EBs with MACHO counterparts have on average shorter periods than those without.

are shown in Figure 34; the figure shows the fraction of matches in magnitude bins of 1 mag; the bin centers range from V =20.5 to 12.5 mag. The error bars are estimated by assuming that the matches in each magnitude bin follow a binomial distribution with probability  $p = x/N_b$ , where x is the number of matches in each magnitude bin and  $N_b$  is the total number of EBs; the error in the expected fraction of matches is then given by equation (3):

$$\sigma_{N_b} = \frac{\sqrt{p(1-p)N_b}}{N_b} = \sqrt{\frac{p(1-p)}{N_b}} \approx \frac{N_b}{N_b - 1} \sqrt{\frac{x/N_b(1-x/N_b)}{N_b}};$$
(3)

in both distributions of Figure 34 the error bar for the brightest magnitude bin is not shown, since in both cases there is only one match, rendering equation (3) meaningless. The figure shows that the fraction of matches increases for brighter magnitudes as expected; the fall at V = 13.5 mag in the distribution of OGLE matches is probably due to small number statistic as evidenced by the large error bar.

#### 5.4. The Small Magellanic Cloud Sample

The same general considerations apply to the SMC sample: the search, performed with the same criteria as the LMC, produced 698 matches. Figure 35 shows the percentage difference of the MACHO and OGLE-II periods versus MACHO period for the matches; Figure 36 shows the histogram of the differences in right ascension and declination.

Unlike the LMC, the sky coverage of the two surveys was approximately the same. Figure 37 shows the positions of the MACHO and OGLE EBs on the sky.

We again investigated why we did not find more matches with OGLE-II. Looking at Figure 37 it is evident that one of the reasons

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TABLE 10 MACHO OGLE-II Matches

Search	No. of Matches
OGLE-II LMC EBs	2580
OGLE-II LMC EBs in MACHO fields	2517
OGLE-MACHO matches	1236
OGLE-II LMC EBs without MACHO counterpart	1281
OGLE-MACHO matches with reported V.	1198
OGLE-II LMC EBs without MACHO counterpart with reported V	1267
MACHO EBs in OGLE fields	1551
MACHO EBs in OGLE fields with OGLE counterpart	1225
MACHO EBs in OGLE fields without OGLE counterpart	326

is the somewhat different sky coverage of the two surveys (MACHO fields 207, 208, and 211 are only partially covered by OGLE), but we also looked for other possible explanations. Again, the most likely explanation is the ways in which the samples were assembled, but we also considered the differences in the distributions of magnitudes and periods. As for the LMC, we compared the distribution of the *V* magnitudes for the 1508 EBs in our sample which have a valid *V* with those of 650 matches and the 666 EBs from OGLE-II without MACHO counterparts (again, these two numbers do not add up to 1351, the size of the OGLE-II sample, because for some EBs the *V* magnitude was not reported). The histograms of these three distributions are shown in Figure 38.

The figure shows that OGLE-II EBs with MACHO counterparts, peaking at  $V \sim 17.5$  mag like the MACHO sample, are on average brighter than those without MACHO counterparts, which is more spread out and roughly constant between 18.5 mag < V < 16.5 mag.

A K-S test shows that these three distributions are different at a >99% confidence level. The behavior at high magnitudes is

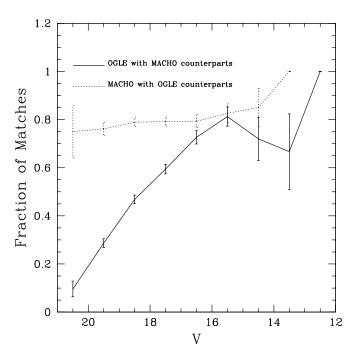


FIG. 34.—*Solid line:* V distribution of the fraction of matches for the OGLE-II LMC EBs in MACHO fields with expected error bars. The magnitude bins are 1 mag wide, and their centers range from V = 20.5 to 12.5 mag. *Dotted line:* V distribution of the fraction of matches for the MACHO LMC EBs in OGLE-II fields.

different for MACHO and OGLE-II: the figure suggests a magnitude limit of  $V \sim 21$  mag for MACHO and  $V \sim 20$  mag for OGLE-II; for V < 19 mag MACHO finds many more EBs than OGLE-II.

We then studied the distributions of the periods: Figure 39 shows that OGLE-II EBs with MACHO counterparts have periods that cluster more in the 1 day < P < 10 days range, as do the MACHO EBs, and a K-S test gives a probability ~43% for the two distribution to be the same. On the other hand OGLE-II EBs without MACHO counterparts have a larger spread of period values, with more objects having P > 10 days and with small "bumps" in the distributions at ~20 and 100 days; a K-S test shows it to be different from both MACHO and OGLE-II MACHO matches at a >99.9% confidence level. The *V* distributions of both the OGLE-II EBs without a MACHO counterparts are shown in Figure 40; the figure shows the fraction of matches in magnitude bins of 1 mag with centers ranging from V = 20.5 to 14.5 mag; the error bars are estimated again by equation (3).

We conclude that differences in sky coverage and techniques used in assembling the samples, as well as different magnitude limits and in general the different behavior at high magnitude of

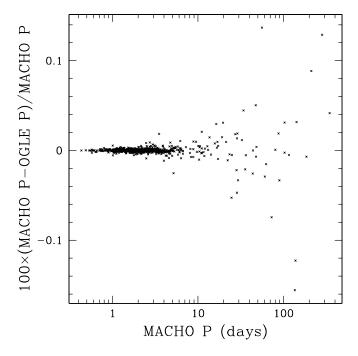


Fig. 35.—Percentage difference for MACHO vs. OGLE-II period for the 698 OGLE-II matches in the SMC sample.

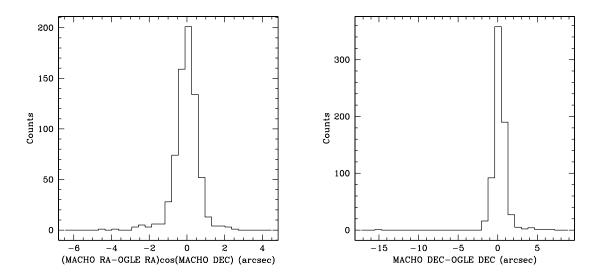


FIG. 36.—Left: Histogram of the differences between right ascensions for 698 OGLE matches in the SMC sample. Right: Histogram of the differences between declinations.

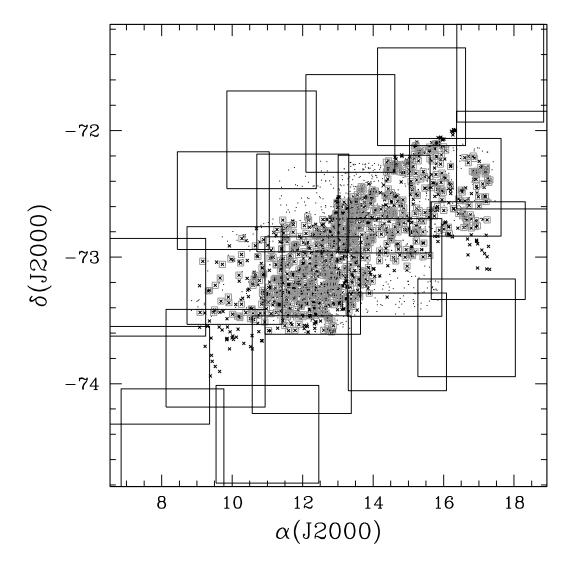


FIG. 37.—Cross-correlation between MACHO and OGLE-II SMC samples. Dots represent MACHO stars, crosses OGLE stars, and gray open boxes the matches.

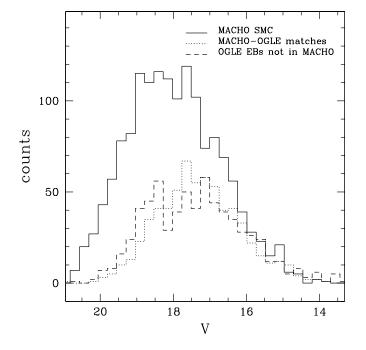


FIG. 38.—*Solid line:* V distribution for 1508 MACHO EBs in the SMC. *Dotted line:* V distribution for 650 OGLE-MACHO matches. *Dashed line:* V distribution for 666 OGLE-II EBs without MACHO counterparts. The figure shows that OGLE-II EBs with MACHO counterparts are on average brighter than those without, and the shape of their V distribution more closely resembles the MACHO V distribution.

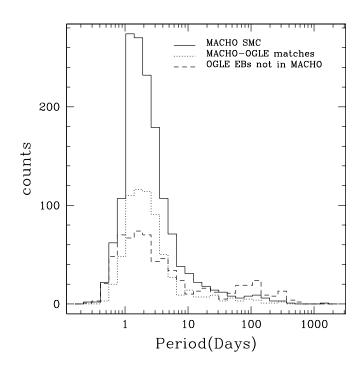


FIG. 39.—*Solid line*: Period distribution for 1508 MACHO EBs in the SMC. *Dotted line*: Period distribution for 650 OGLE-MACHO matches. *Dashed line*: Period distribution for 666 OGLE-II EBs without MACHO counterparts. The figure shows that both MACHO and OGLE-II EBs with MACHO counterparts have periods that cluster more in the 1 day < P < 10 days range. OGLE EBs without MACHO counterparts have a larger spread in period and smaller "bumps" in the distribution at ~20 and 100 days.

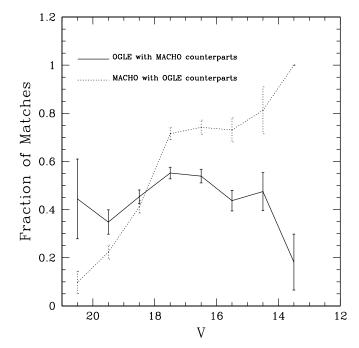


FIG. 40.—*Solid line:* V distribution of the fraction of matches of matches for the OGLE-II SMC EBs in MACHO fields with expected error bars. The magnitude bins are 1 mag wide, and their centers range from V = 20.5 to 13.5 mag. *Dotted line:* V distribution of the fraction of matches for the MACHO SMC EBs in OGLE-II fields.

the two surveys, all play a role in not finding an higher number of OGLE-II counterparts to our sample; the fact that the SMC was less observed than the LMC by MACHO may also explain why we find fewer long-period objects, while the fact that the exposure time for the SMC was double that of the LMC (Alcock et al. 1999) may explain why we find many faint objects.

## 6. THE DATA ONLINE

The data presented in this paper can be accessed online at the *Astronomical Journal* Web site<sup>14</sup> and are mirrored at the Harvard University Initiative in Innovative Computing (IIC)/Time Series Center.<sup>15</sup>

At both sites the data consist of a summary table for each cloud and light curves for all the EBs in the samples. The light-curve files contain the *unfolded* data in MACHO magnitudes; these same files can also be retrieved from the MACHO Web site. Finally, for the LMC the input and output files used in the JKTEBOP fits are provided.

This work uses public domain data from the MACHO project, whose work was performed under the joint auspices of the US Department of Energy, National Nuclear Security Administration by the University of California, Lawrence Livermore National Laboratory, under contract W-7405-Eng-48, the National Science Foundation through the Center for Particle Astrophysics of the University of California under cooperative agreement AST 88-09616, and the Mount Stromlo and Siding Spring Observatory, part of the Australian National University. This work uses public domain data obtained by the OGLE project. We are

<sup>&</sup>lt;sup>14</sup> See http://www.journals.uchicago.edu/AJ/.

<sup>&</sup>lt;sup>15</sup> See http://timemachine.iic.harvard.edu; http://timemachine.iic.harvard.edu/ faccioli/ebs/.

program. We thank the referee for many helpful suggestions. L. F. acknowledges the kind hospitality of the Institute of Geophysics and Planetary Physics at Lawrence Livermore National Laboratory and of the Harvard-Smithsonian Center for Astrophysics, where part of the work was done.

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